

- 2. (a)** Show that $f(x) = x^4 + x - 1$ has a real root α in the interval $[0.5, 1.0]$. **(2)**

- (b)** Starting with the interval $[0.5, 1.0]$, use interval bisection twice to find an interval of width 0.125 which contains α . **(3)**

- (c)** Taking 0.75 as a first approximation, apply the Newton Raphson process twice to $f(x)$ to obtain an approximate value of α . Give your answer to 3 decimal places. **(5)**



3. A parabola C has cartesian equation $y^2 = 16x$. The point $P(4t^2, 8t)$ is a general point on C .

(a) Write down the coordinates of the focus F and the equation of the directrix of C . (3)

(b) Show that the equation of the normal to C at P is $y + tx = 8t + 4t^3$. (5)



6. (a) Prove by induction

$$\sum_{r=1}^n r^3 = \frac{1}{4}n^2(n+1)^2 \quad (5)$$

(b) Using the result in part (a), show that

$$\sum_{r=1}^n (r^3 - 2) = \frac{1}{4}n(n^3 + 2n^2 + n - 8) \quad (3)$$

(c) Calculate the exact value of $\sum_{r=20}^{50} (r^3 - 2)$. (3)



Question 7 continued

A series of horizontal lines for writing an answer to Question 7.

(Total 7 marks)

Q7



